

Internal Validation of the Mathematical Model $v_s = EV_r + FI_r$ as Applied to a Three-Phase Medium Transmission Lines Characterized by Unbalance Shunt Circuit

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Abstract—In the previous research, the researcher showed the derivation of mathematical models expressing sending voltage and sending current in terms of receiving voltage and receiving current. Hence, two mathematical models for a three phase medium transmission lines which includes $V_s = EV_r + FI_r$ and $I_s = GV_r + HI_r$ are developed. This research is now after for the internal validation of $V_s = EV_r + FI_r$ using t-test for independent sample means at 1% level of significance.

Index Terms—Internal validity, mathematical model, power system, transmission lines.

I. INTRODUCTION

Understanding of mathematical models for electricity is important. The future electrical engineers can use his knowledge on the model to explain and understand electrical phenomenon. Knowledge on the mathematical models is a valuable tool in solving work related problem work and many practical situations related to electricity.

The mathematical models for three-phase medium transmission lines characterized by unbalanced shunt admittance are derived using Kirchhoff's law and algebraic manipulation. The circuit diagram and the mathematical model are shown below [1]

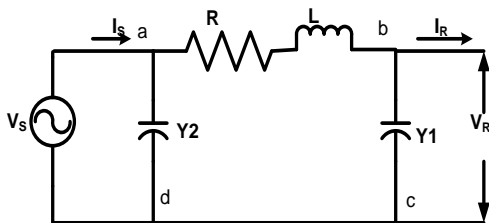


Fig. 1. Circuit diagram of short transmission line per phase.

$$V_s = EV_r + FI_r \tag{1}$$

$$I_s = GV_r + HI_r \tag{2}$$

where:

$$E = (1 + ZY_1) \tag{3}$$

$$F = Z \tag{4}$$

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$$H = ZY_2 + 1 \tag{5}$$

$$G = EY_2 + Y_1 \tag{6}$$

The three electrical parameters of a three phase medium transmission lines are resistance, inductance and capacitance. The mathematical models of the three electrical parameters are given below [2]-[6]

$$R = \frac{\rho l}{A} \tag{7}$$

$$X_L = 2\pi fL \tag{8}$$

$$X_C = \frac{1}{2\pi fC} \tag{9}$$

$$Y = \frac{1}{X_C} \tag{10}$$

The main objective of the study is the internal validation of the first mathematical models expressing the source voltage in terms of the receiving voltage and receiving current ($V_s = EV_r + FI_r$). The specific objectives are the following:

- 1) to design a simple experiment and measure sending voltage using NI Multi-Sim
- 2) to calculate the sending voltage using $V_s = EV_r + FI_r$
- 3) to validate the mathematical model which express source voltage in terms of receiving voltage and receiving current using t-test for independent sample means.

For the scope and limitation, the study covers internal validation of the model. The model is validated by comparing the calculated and measured sending voltage using t test for independent sample means at 1% level of significance and sample size of 10.

For the significance of the study, the internal validation on the research is another material that can be used in the laboratory by the engineering educators as a laboratory experiment for transmission line.

II. DISCUSSION AND RESULTS

Internal validity in research means that the change in the dependent variable (output variable) is due to the changes in the independent variable. The block diagram below showed the independent variables, input variables and output variables.

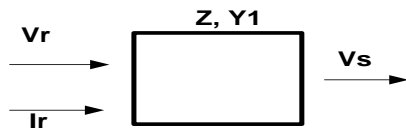


Fig. 2. Block diagram for the mathematical model $V_s = EV_r + F I_r$.

Y_1 and Z are independent variables.
 V_r and I_r are the input variables
 V_s is the output variables.

A. Design a Simple Experiment Using NI Multi-Sim for the Mathematical Models $V_s = EV_r + F I_r$

- 1) Set the electrical parameters such as Resistor (R), Inductor (L) and Capacitor (C) for a 50 miles transmission lines.

$$R = 4.705 \Omega$$

$$L = 50.35 \text{ mH}$$

$$C1 = .163 \mu\text{F}$$

$$C2 = 1.6291 \mu\text{F}$$

- 2) Construct the circuit diagram below using Ni MultiSIM. Please refer to Fig. 1.

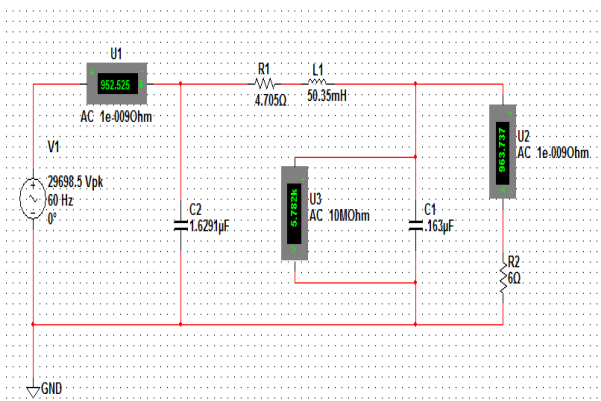


Fig. 3. Circuit diagram of short transmission line per phase for the first mathematical model using NI multisim.

- 3) Set the value of sending voltage to $\sqrt{2}$ (V_1) from Table I and frequency to 60 Hz.

TABLE I: DIFFERENT VALUES OF SENDING VOLTAGE FOR PROCEDURE C

TRIALS	V_s	V_r (V)	I_r (A)
1	21000		
2	22000		
3	23000		
4	24000		
5	25000		
6	26000		
7	27000		
8	28000		
9	29000		
10	30000		

- 4) Press Simulate.
- 5) Measure the receiving voltage (V_r) and receiving current (I_r). Repeat procedure A to D for the 2nd to 10th trial.
- 6) Supply the data needed in the Table II.

TABLE II: EXPECTED MEASURED SENDING VOLTAGE AND RECEIVING CURRENT USING NI MULTI SIM. MEASUREMENT OF V_r AND I_r CAN BE VERIFIED USING NI MULTISIM

TRIALS	V_s	V_r	I_r
1	21000	5782	963.737
2	22000	6058	1010
3	23000	6333	1056
4	24000	6608	1101
5	25000	6884	1147
6	26000	7159	1193
7	27000	7435	1239
8	28000	7710	1285
9	29000	7985	1331
10	30000	8261	1377

B. Solve for the Sending Voltage Using the First Model

- 1) Set the value of R , L and C

$$R = 4.705 \text{ mi}$$

$$L = 50.35 \text{ mH}$$

$$C_T = 1.792 \mu\text{F}$$

- 2) C_1 and C_2 are divided so that combined reactance will result to $1.792 \mu\text{F}$

$$C_1 = \left(\frac{1}{11}\right)(1.792 \mu\text{F})$$

$$C_1 = 0.163 \mu\text{F}$$

$$C_2 = C_T - C_1$$

$$C_2 = 1.792 \mu\text{F} - 0.163 \mu\text{F}$$

$$C_2 = 1.6291 \mu\text{F}$$

solve for X_{c1} and X_{c2}

$$X_{c1} = \frac{1}{2\pi f C}$$

$$X_{c1} = \frac{1}{(2\pi)(60)(.163 \mu\text{F})}$$

$$X_{c1} = -16273.51184j$$

$$X_{c2} = -16273.51184j$$

solve for Y_1

$$Y_1 = \frac{1}{X_c}$$

$$Y_1 = \frac{1}{-16273.511i}$$

- 3) Solve for the calculated value of the sending voltage using the measured value of receiving voltage and receiving current from Table III. The theoretical value of phase angle -60.598 is also used.

$$V_r = 5782 \angle -60.598$$

$$I_r = 963.737 \angle -60.598$$

Solution

$$V_s = EV_r + FI_r$$

solve for E

$$E = (1 + ZY_1)$$

$$E = 1 + (4.705 + 18.982i) \left(\frac{1}{-16273.511i} \right)$$

$$E = .999 \angle 0.0165$$

solve for F

$$F = Z$$

$$F = 4.705 + 18.982i$$

substitute A and B to $V_s = EV_r + FI_r$

$$V_s = (.999 \angle .0165)(5782 \angle -60.598) + (4.705 + 18.982i)(963.72 \angle -60.598)$$

$$V_s = 20968.427$$

- 4) Following the same procedures for different source voltage of Table III.

TABLE III: EXPECTED MEASURED VERSUS CALCULATED SENDING VOLTAGE

TRIALS	Calculated V_s	Measured V_s
1	20968.427	21000
2	22007.6	22000
3	23009.5	23000
4	23992.5	24000
5	24994.86	25000
6	25996.74	26000
7	26999.108	27000
8	28001	28000
9	29016.89	29000
10	30000.41	30000

C. Internal Validation of the Mathematical Model

$V_s = EV_r + FI_r$ at 1% Level of Significance

- 1) Using Microsoft Excel Data analysis calculates the variance of the two independent samples.

TABLE IV: F TEST OF TWO SAMPLE FOR VARIANCES

F-Test Two-Sample for Variances		
	Variable 1	Variable 2
Mean	25500	25498.7
Variance	9166667	9203732
Observations	10	10
df	9	9
F	0.995973	
P(F<=f) one-tail	0.497651	
F Critical one-tail	0.186876	

Table IV shows the variances of the calculated and measured sending voltage are different at 1 % level of significance.

- 2) State the hypotheses and identify the claim based on Table III.

H_0 : The mean of calculated sending voltage is equal to the mean of measured sending voltage (claim)

H_1 : The mean of calculated voltage is not equal to the mean of measured voltage

- 3) Apply Microsoft excel analysis in the data of Table III

TABLE V: T-TEST: TWO-SAMPLE WITH UNEQUAL VARIANCES

	Variable 1	Variable 2
Mean	25500	25498.704
Variance	9166667	9203732.2
Observations	10	10
Hypothesized Mean Difference	0	
df	18	
t Stat	0.000957	
P(T<=t) one-tail	0.499624	
t Critical one-tail	2.55238	
P(T<=t) two-tail	0.999247	
t Critical two-tail	2.87844	

- 4) Make the decision. Accept the null hypothesis since .000957 falls on non-critical region.

- 5) Summarize the results. There is enough evidence to support the researcher's claim that the calculated value is equal to the measured value at 1% level of significance.

III. CONCLUSIONS AND DIRECTIONS FOR FUTURE USE

The model $V_s = EV_r + FI_r$ is internally valid at 1% level of significance using the t test for two independent samples which means that the calculated values are equal to the measured values. Hence the mathematical model is effective in predicting the value of the source voltage and source

current given the receiving electrical parameters I_r and V_r .

The researcher recommends the internal validation in the research as an equivalent experiment to compare the theoretical and actual value.

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